

# A Method Selection Framework for Operating-Profile Assessment and Sensitivity Analysis of DC/AC Inverters in Photovoltaic Plants

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# Motivation: why inverter operating profiles matter

The inverter is not only a DC/AC converter; it is an active monitoring and control node.

## Operational complexity

Irradiance, temperature, DC inputs, grid conditions, control settings and alarms interact over time.

## Decision problem

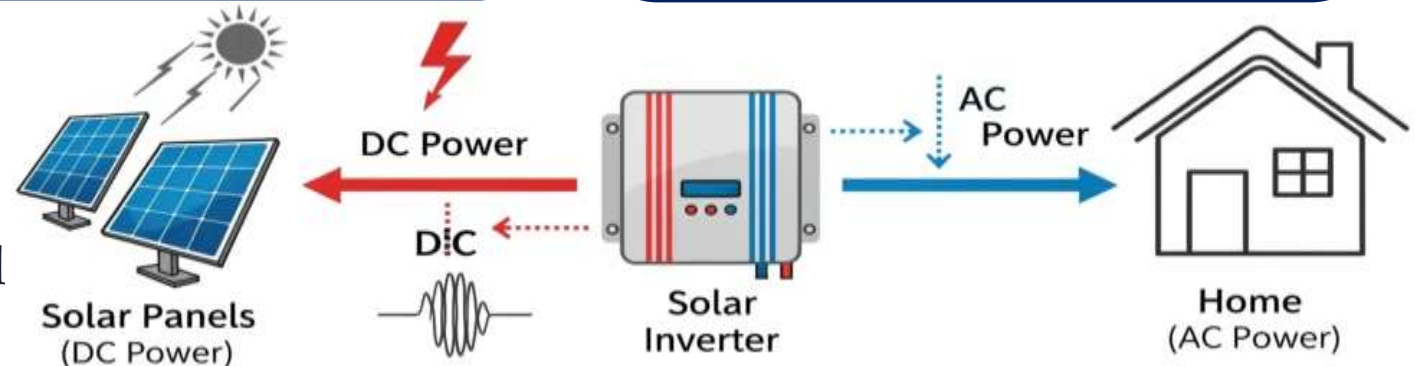
Many assessment and sensitivity methods exist, but their suitability depends on data quality and purpose.

## Research contribution

A formal framework selects the method family that best supports monitoring, diagnostics and sustainable control.

## Three guiding questions

1. How to formalize the operating profile mathematically?
2. Which methods fit different data and model maturity levels?
3. How to translate sensitivity results into O&M actions?



**Goal:  $\mathcal{D} \rightarrow KPI \rightarrow Sensitivity \rightarrow O\&M\ decision$**

**Key message: Method selection comes before detailed engineering actions**

# Mathematical object: the inverter operating profile

## Observation interval

$$\mathcal{T} = [t_0, t_N], t_k = t_0 + k\Delta t, k = 0, 1, \dots, N \quad (1)$$

$t_0$  is the starting time of observation

$t_N$  is the ending time

$\Delta t$  is the sampling time interval

## Structured definition

$$\mathcal{OP} = (\mathcal{T}, \mathbf{U}, \mathbf{X}, \mathbf{Y}, \mathbf{M}, \boldsymbol{\theta}, \boldsymbol{\Omega}, \mathbf{K}) \quad (3)$$

$\mathcal{T}$  is the observation time interval

$\mathbf{U} = \{\mathbf{u}_k\}_{k=0}^N$  is the input data matrix

$\mathbf{X} = \{\mathbf{x}_k\}_{k=0}^N$  is the matrix of internal states

$\mathbf{Y} = \{\mathbf{y}_k\}_{k=0}^N$  is the matrix of output indicators

In discrete form, the work profile is represented as a set of observations

$$\mathcal{D} = \{\mathbf{u}_k, \mathbf{x}_k, \mathbf{y}_k, \mathbf{m}_k\}_{k=0}^N \quad (2)$$

$\mathbf{u}_k$  is the vector of input quantities at time  $t_k$

$\mathbf{x}_k$  is the vector of internal states of the inverter

$\mathbf{y}_k$  is the vector of output indicators

$\mathbf{m}_k$  is a vector or label of the operating mode

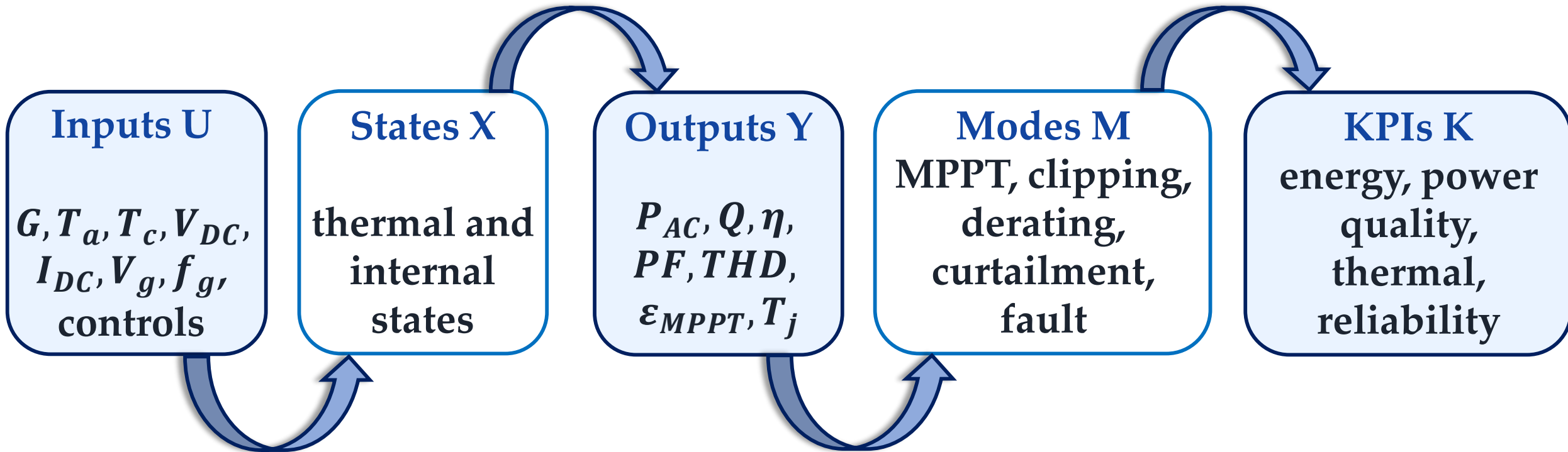
$\mathbf{M} = \{\mathbf{m}_k\}_{k=0}^N$  is the sequence of operating modes

$\boldsymbol{\theta}$  is the vector of inverter parameters

$\boldsymbol{\Omega}$  is the area of permissible work

$\mathbf{K}$  is the vector of aggregated KPIs

# Mathematical object: the inverter operating profile



This formal object links measured time series, physical constraints and decision indicators in one notation.

# KPI apparatus: from measurements to indicators

## Power and efficiency

$$P_{dc}(t) = V_{dc}(t)I_{dc}(t) \quad (4)$$

$$\eta(t) = \frac{P_{ac}(t)}{P_{dc}(t)}, P_{dc}(t) > 0 \quad (5)$$

$P_{ac}(t)$  is the active AC power

$V_{dc}(t)$  is the DC voltage at the inverter input

$I_{dc}(t)$  is the DC input current

$P_{dc}(t)$  is the DC input power

$\eta(t)$  is the instantaneous conversion efficiency of the inverter

## Energy-weighted efficiency

$$E_{ac} \approx \sum_{k=0}^N P_{ac,k} \Delta t, E_{dc} \approx \sum_{k=0}^N P_{dc,k} \Delta t \quad (6)$$

$$\bar{\eta}_E = \frac{E_{ac}}{E_{dc}}, \quad E_{dc} > 0 \quad (7)$$

$E_{ac}$  is the AC energy produced

$E_{dc}$  is the DC input energy

$\bar{\eta}_E$  is the average energy efficiency

# KPI apparatus: from measurements to indicators

## Loss separation

$$E_{clip} \approx \sum_{k=0}^N \max(0, P_{ac,k}^* - P_{rated}) \Delta t \quad (8)$$

$$E_{der} = \sum_{k=0}^N \left( P_{ac,k}^{ref}(t) - P_{ac,k}(t) \right)_+ \Delta t \quad (9)$$

$E_{clip}$  is the clipping loss

$E_{der}$  is the derating energy

## Indices

$$CI = \frac{E_{clip}}{E_{ac} + E_{clip}} \quad (10)$$

$$DI = \frac{E_{der}}{E_{ac} + E_{der}} \quad (11)$$

$CI$  is the clipping index

$DI$  is the derating index

**Interpretation: clipping, derating and curtailment must be separated before diagnosing inverter faults.**

## KPI families

Energy · MPPT · limitation · power quality · thermal · reliability · sustainability

## Mode-dependent interpretation: same number, different meaning

$$\mathcal{M} = \{M_0, M_1, M_2, M_3, M_4, M_5, M_6, M_7\} \quad (12)$$

$M_0$ : off mode or night mode

$M_1$ : start

$M_2$ : normal MPPT operation

$M_3$ : clipping

$M_4$ : thermal derating

$M_5$ : curtailment by external command

$M_6$ : network limitation or deviation

$M_7$ : failure, alarm or protective shutdown

## Conditional sensitivity

$$S_i^{Y|M_q} = S(Y, X_i | M = M_q) \quad (13)$$

**Estimate sensitivity within the relevant operating mode,  
not across mixed modes.**

# Mode-dependent interpretation: same number, different meaning

## During MPPT

Low  $\frac{\partial P_{AC}}{\partial G}$  may indicate MPPT, string, shading or soiling issues.

## During clipping

Low  $\frac{\partial P_{AC}}{\partial G}$  is expected because AC output is limited by  $P_{rated}$ .

## During curtailment

Low  $\frac{\partial P_{AC}}{\partial G}$  reflects external power command or grid constraint, not necessarily a fault.

$$S_G^{P_{AC}|M_{clip}} \approx 0 \not\Rightarrow MPPT \text{ fault} \quad (14)$$

# Data quality as a mathematical gatekeeper

$$Q_D = w_1 C_D + w_2 A_D + w_3 S_D + w_4 K_D + w_5 M_D - w_6 E_D \quad (15)$$

**C**

completeness

**A**

accuracy

**S**

synchronization

**K**

calibration

**M**

metadata/modes

**E**

bad records

## Eligible method classes by data maturity

Level	Typical condition	Suitable methods
Low	missing irradiance or unsynchronized channels	QA/QC, limited KPI review
Medium	basic SCADA: P, V, I, G, T; incomplete flags	KPI, regression, benchmarking
High	timestamps, mode labels, metadata and alarms	local sensitivity, Morris, fleet monitoring
Very high	calibrated model and distributions	Sobol/Saltelli, Monte Carlo, ML, digital twin

$$\mathcal{M}_{feas} = \{M_m: Q_D \geq q_{min}(M_m)\} \quad (16)$$

# Method-selection framework: score, feasibility, hierarchy

$$Score_m = w_A A_m + w_I I_m + w_D D_m + w_R R_m + w_{OM} OM_m + w_S S_m - w_C C_m \quad (17)$$

$$M^* = \arg \max_{M_m \in \mathcal{M}_{feas}} Score_m \quad (18)$$

## Practical hierarchy



## Scenario-to-method examples

Scenario	Recommended method
Commissioning	KPI + residual analysis + local sensitivity
Many uncertain factors	Morris screening before expensive global analysis
Global risk analysis	Sobol/Saltelli + Monte Carlo
Large inverter fleet	ML/SHAP + fleet benchmarking, only with enough history

# Sensitivity analysis toolbox: local, screening, global

## Local sensitivity

Best for commissioning and control tuning near one operating point.

$$S_i^Y = \frac{X_i}{Y} \frac{\partial Y}{\partial X_i} \approx \frac{X_i}{Y} \frac{F(X_i + \Delta X_i) - F(X_i)}{\Delta X_i} \quad (19)$$

## Morris screening

Finds important factors at low computational cost when the factor list is long.

$$EE_i = \frac{F(X_1, \dots, X_i + \Delta, \dots, X_n) - F(X_1, \dots, X_i, \dots, X_n)}{\Delta}$$

$$\mu_i^* = \frac{1}{r} \sum_{q=1}^r |EE_i^{(q)}| \quad (20)$$

## Sobol/Saltelli

Explains output variance and interactions for calibrated models.

$$S_i = \frac{\text{Var}_{X_i}(E[Y|X_i])}{\text{Var}(Y)}$$

$$S_{T_i} = 1 - \frac{\text{Var}_{X_{\sim i}}(E[Y|X_{\sim i}])}{\text{Var}(Y)} \quad (21)$$

Interpretation rule: If  $S_{T_i} \gg S_i$ , the factor contributes mainly through interactions.

## Factor groups for O&M communication

$$\mathbf{X} = [\mathbf{X}_{clim}, \mathbf{X}_{DC}, \mathbf{X}_{grid}, \mathbf{X}_{thermal}, \mathbf{X}_{ctrl}] \quad (22)$$

Climate → resource and thermal variability

DC side → MPPT and string behavior

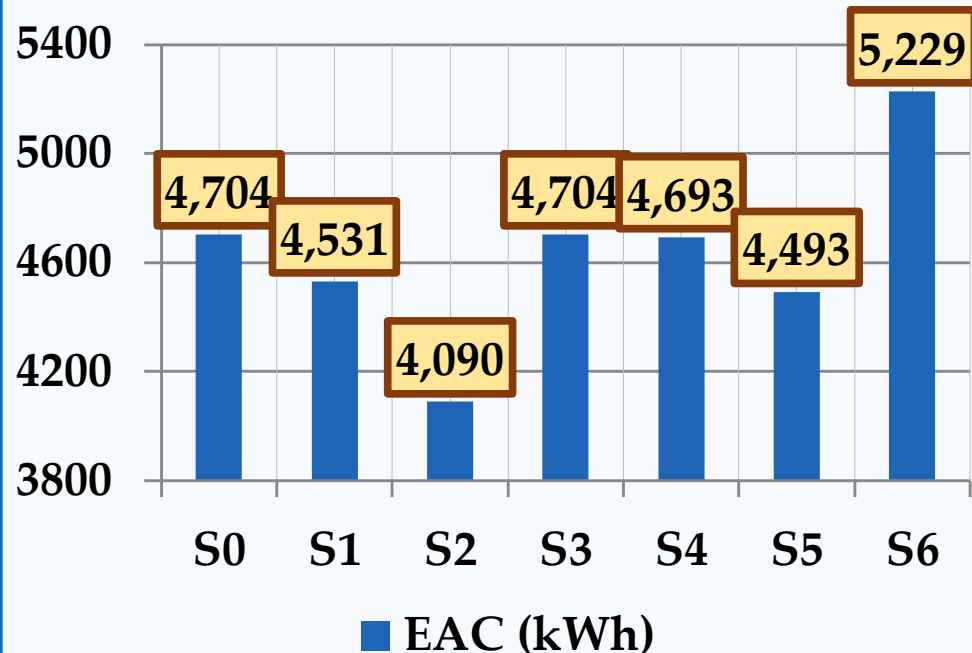
Grid → PF, reactive power and THD

Thermal/control → derating, lifetime and settings

# Numerical workflow: scenario diagnostics for a 100 kW inverter

$$P_{AC,rated} = 100kW, P_{DC,inst} = 120/135kWp, \Delta t = 5min, N = 2016$$

Delivered AC energy by scenario



Scenario	Diagnostic signal	Interpretation
S1	$T_{jmax} = 92.9\text{ }^{\circ}\text{C};$ $DI = 0.48\%$	Thermal/cooling risk
S2	$EAC = 4090.3\text{ kWh};$ $PR = 74.09\%$	Shading/soiling or MPPT degradation
S3	$PF_w = 0.977;$ $THD_w = 2.43\%$	Grid-voltage stress
S5	$CuI = 4.49\%;$ $\eta_E = 93.58\%$	Curtailment, not inverter fault
S6	$EAC = 5229.1\text{ kWh};$ $CI = 1.51\%$	Higher ILR, but clipping appears

The workflow separates loss mechanisms before ranking influential factors.

# Global sensitivity ranking: Sobol total indices

## Total Sobol indices $S_{T_i}$ from the illustrative model

Factor	$P_{AC}$	$\eta$	$THD$	$T_j$	$PF$
$G$	0.970	0.113	0.648	0.505	0.000
$T_a$	0.029	0.340	0.020	0.480	0.000
$V_g$	0.000	0.000	0.045	0.000	1.000
$r_{DC}$	0.000	0.420	0.241	0.001	0.000
$R_{eq}$	0.000	0.000	0.000	0.023	0.000
$f_{sw}$	0.000	0.122	0.051	0.000	0.000

### Interpretation

$P_{AC}$  is dominated by irradiance  $G$ .

$\eta$  is driven by DC ripple  $r_{DC}$ , temperature  $T_a$  and switching frequency  $f_{sw}$ .

$THD$  is mainly load/irradiance plus ripple.

$T_j$  is explained by  $G$  and  $T_a$ .

$PF$  is almost entirely controlled by grid voltage  $V_g$ .

$S_{T_i} \gg S_i \Rightarrow$  *interaction effect*

Relevant factors depend on the selected output indicator — there is no universal ranking.

## From mathematical sensitivity to O&M action

$$Risk_l = a_1 DI_l + a_2 \overline{THD}_l + a_3(1 - \overline{PF}_l) + a_4(1 - HI_l) + a_5 N_{alarm,l} \quad (23)$$

$$|S_i^{K_j}| > \lambda_{i,j} \Rightarrow O\&M \text{ Action}_{i,j} \quad (24)$$

Sensitivity pattern	Likely cause	Recommended action
High $S(\eta, T_a)$	Cooling degradation or increased losses	Inspect fans, heat sinks, airflow and derating logic
High $S(THD, ripple)$	DC-link degradation or filter issue	Check capacitors, ESR and output filter condition
Low $S(P_{AC}, G)$ in normal mode	MPPT problem, shading or soiling	Inspect strings and MPPT channels
High $S(PF, V_g)$	Grid-voltage effect or $Q/PF$ setting issue	Verify $Q(V)$ and power-factor control parameters

**Actionability is the final criterion: a sensitivity index is useful only if it can trigger a meaningful technical decision.**

# Conclusions

## Sustainable control objective

$$J = w_1(1 - \eta_E) + w_2THD + w_3 \max(0, T_j - T_{lim}) + w_4DI + w_5CI - w_6E_{AC} \quad (25)$$

## Recommended practical sequence

$$KPI + \textit{Conditional Regression} + \textit{Local Sensitivity} + \textit{Morris} + \textit{Sobol} + \textit{ML/Hybrid} \quad (26)$$

1

Define OP formally: inputs, states, outputs, modes, constraints and KPIs.

2

Filter by data quality before applying complex models.

3

Interpret sensitivities conditionally by operating mode.

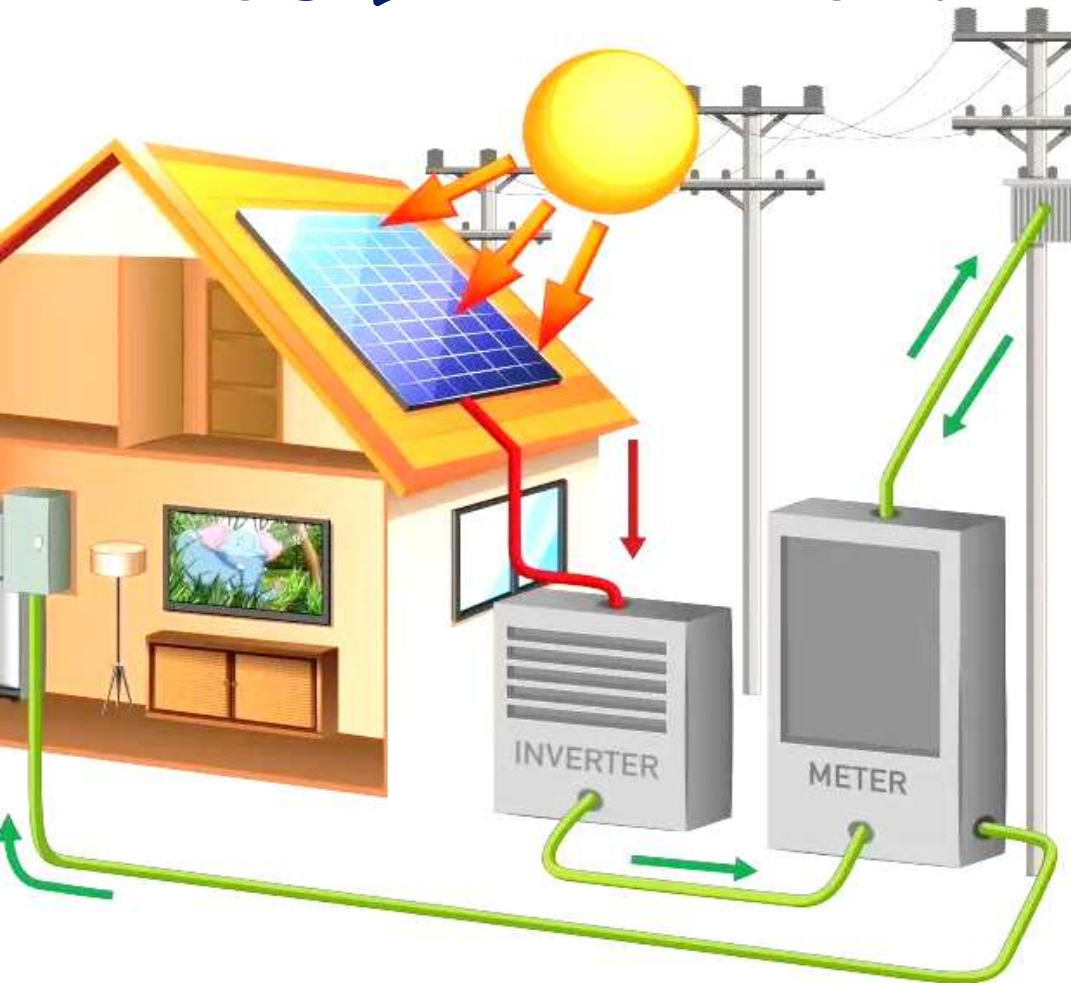
4

Translate rankings into diagnostics, maintenance and control tuning.

5

Balance yield, power quality, thermal risk, reliability and lifetime.

# THANK YOU FOR YOUR ATTENTION!



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