

Hierarchy of sigmoid growth models – towards justification of sigmoid treatment of nucleation data

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Introduction:

The hierarchy of sigmoid growth models (HSGM), built for first time in Kleshtanova et al, Crystals 2023, 13, 1690.

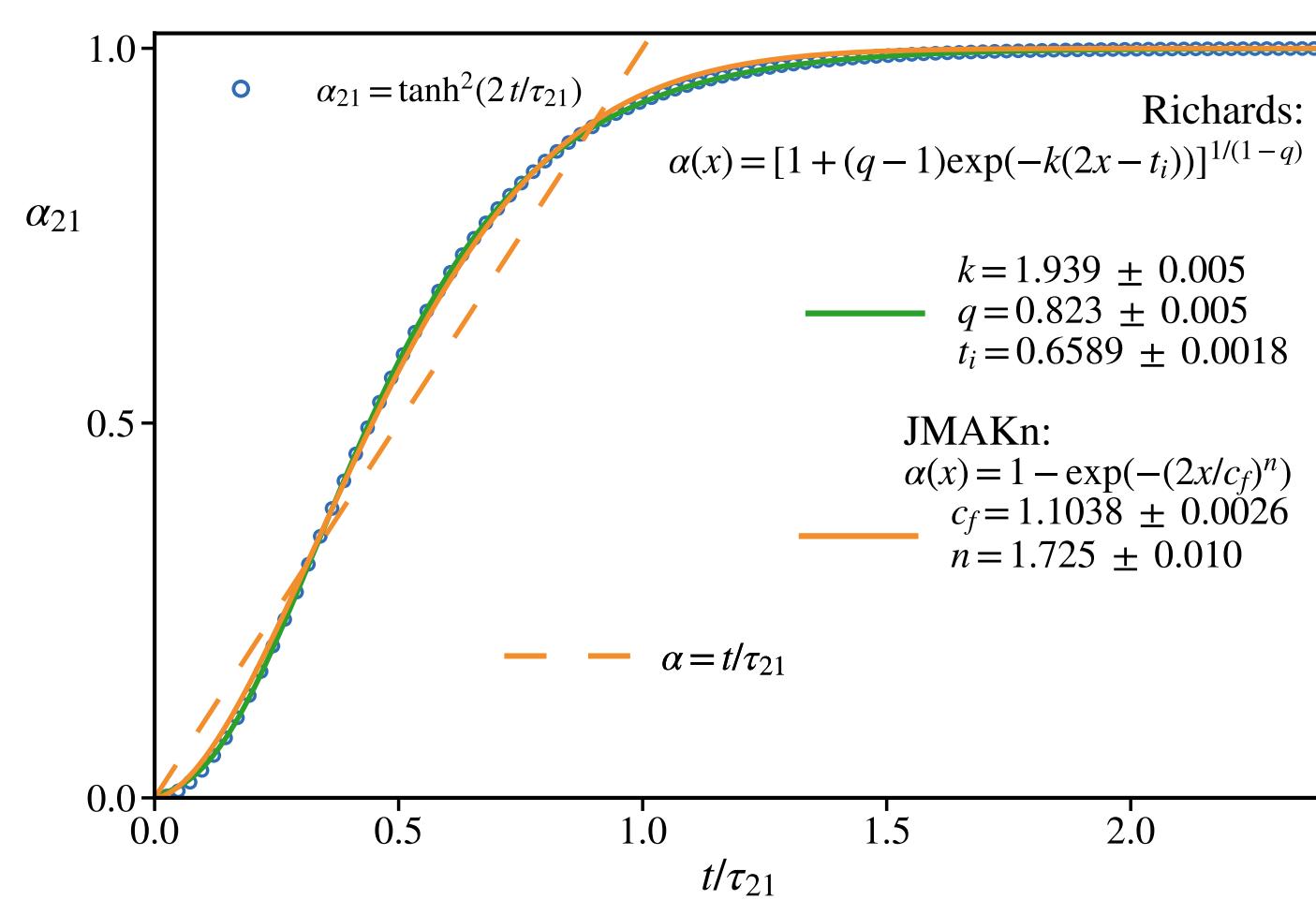
Consists for the moment of 3 models with increasing complexity: α_{Dg} , Johnson-Mehl-Avrami-Kolmogorov (JMAKn) and Richards models

Here we give the equations of the three models from the HSGM for the transformation ratio α :

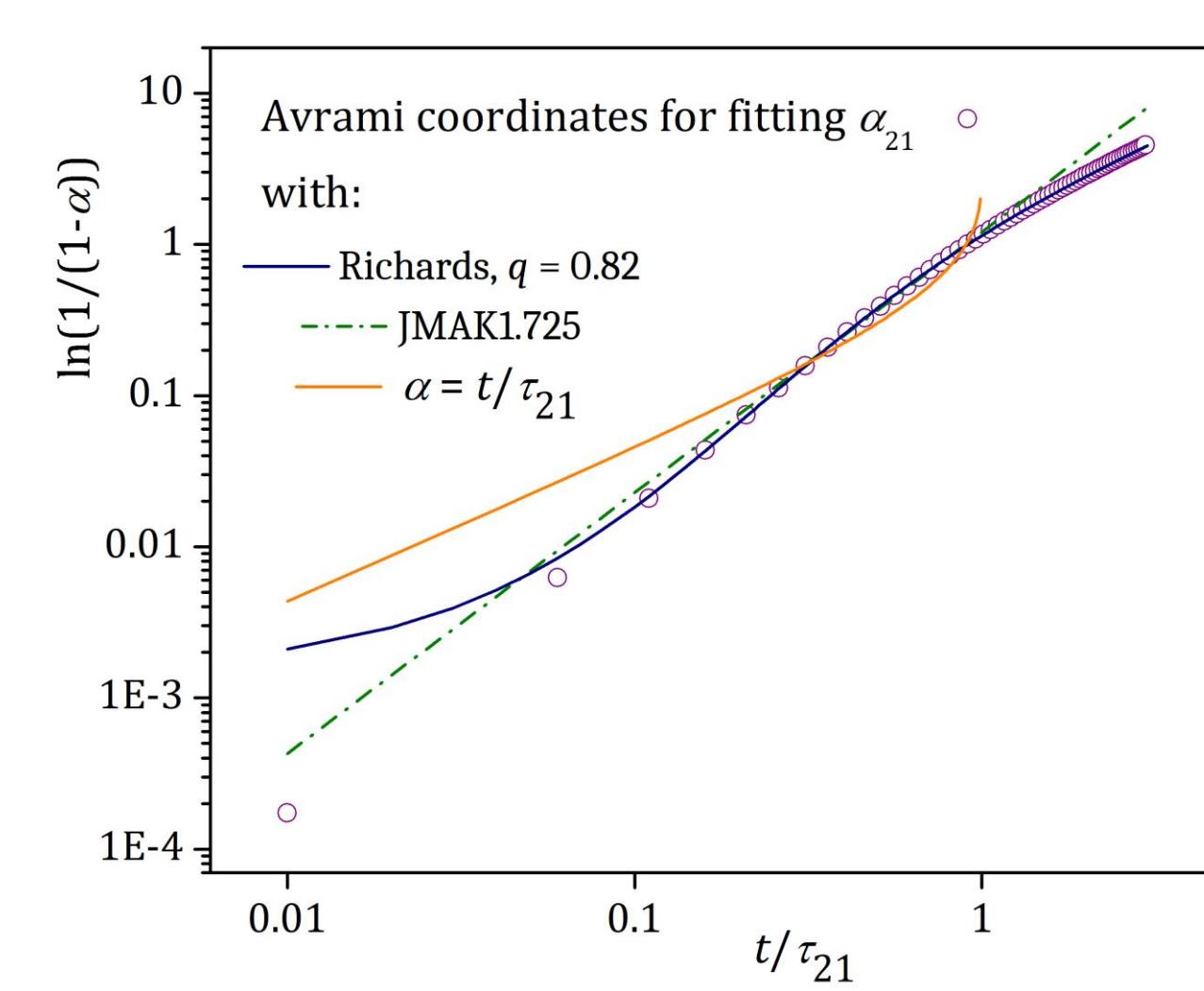
1) $\alpha_{Dg} : d\alpha_{Dg} / d(t/\tau) = 2D(\alpha_{Dg})^{(D-1)/D}(1-\alpha_{Dg})^g; \alpha_{21} = \tanh 2(t/\tau_{21})$ (with 1 parameter!)

2) JMAKn: $\alpha = 1 - \exp[-(t/\tau_{av})^q]$ (with 2 parameters!)

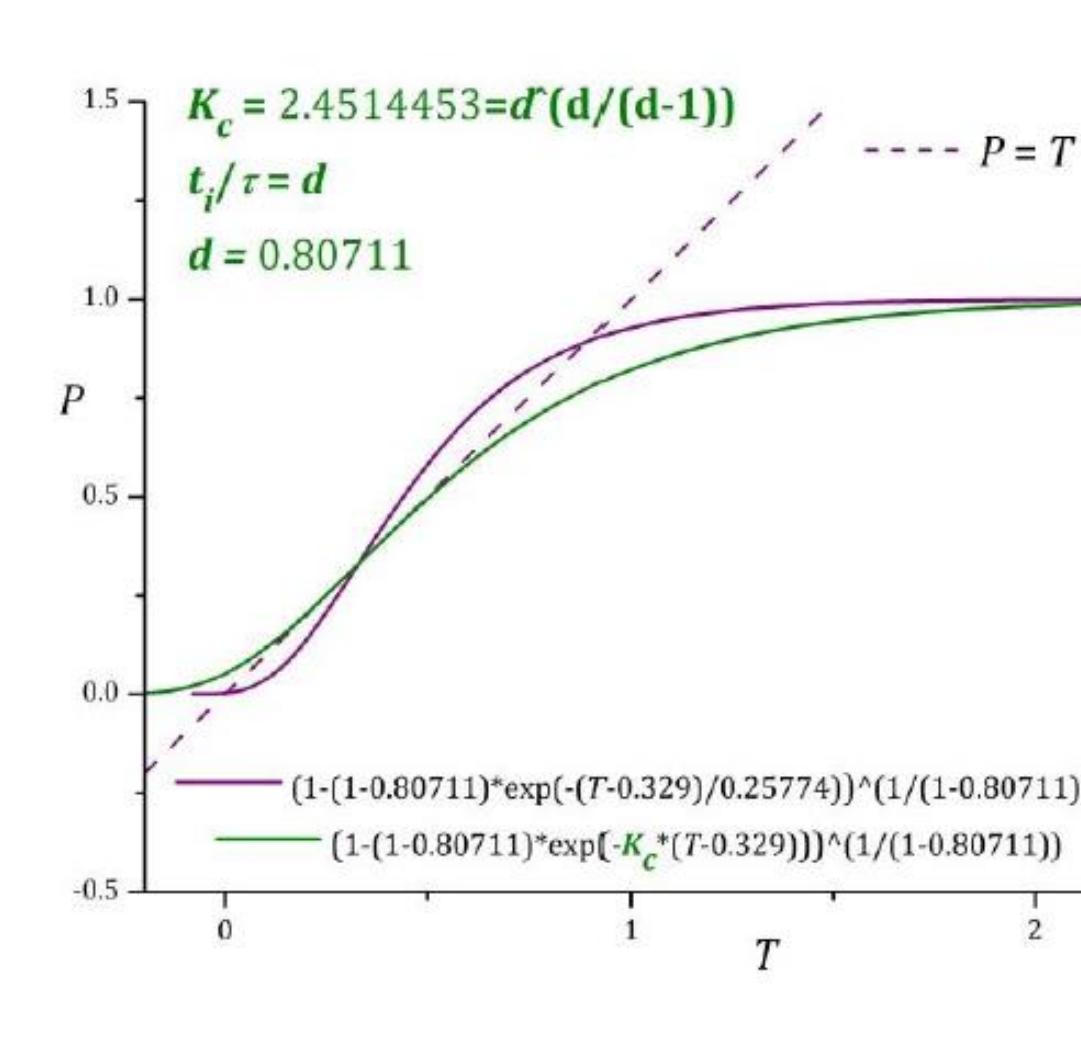
3) Richards: $\alpha = \{1 + (q-1)\exp[-(t-t_i)/t_k]\}^{1/(1-q)}$ (with 3 parameters)



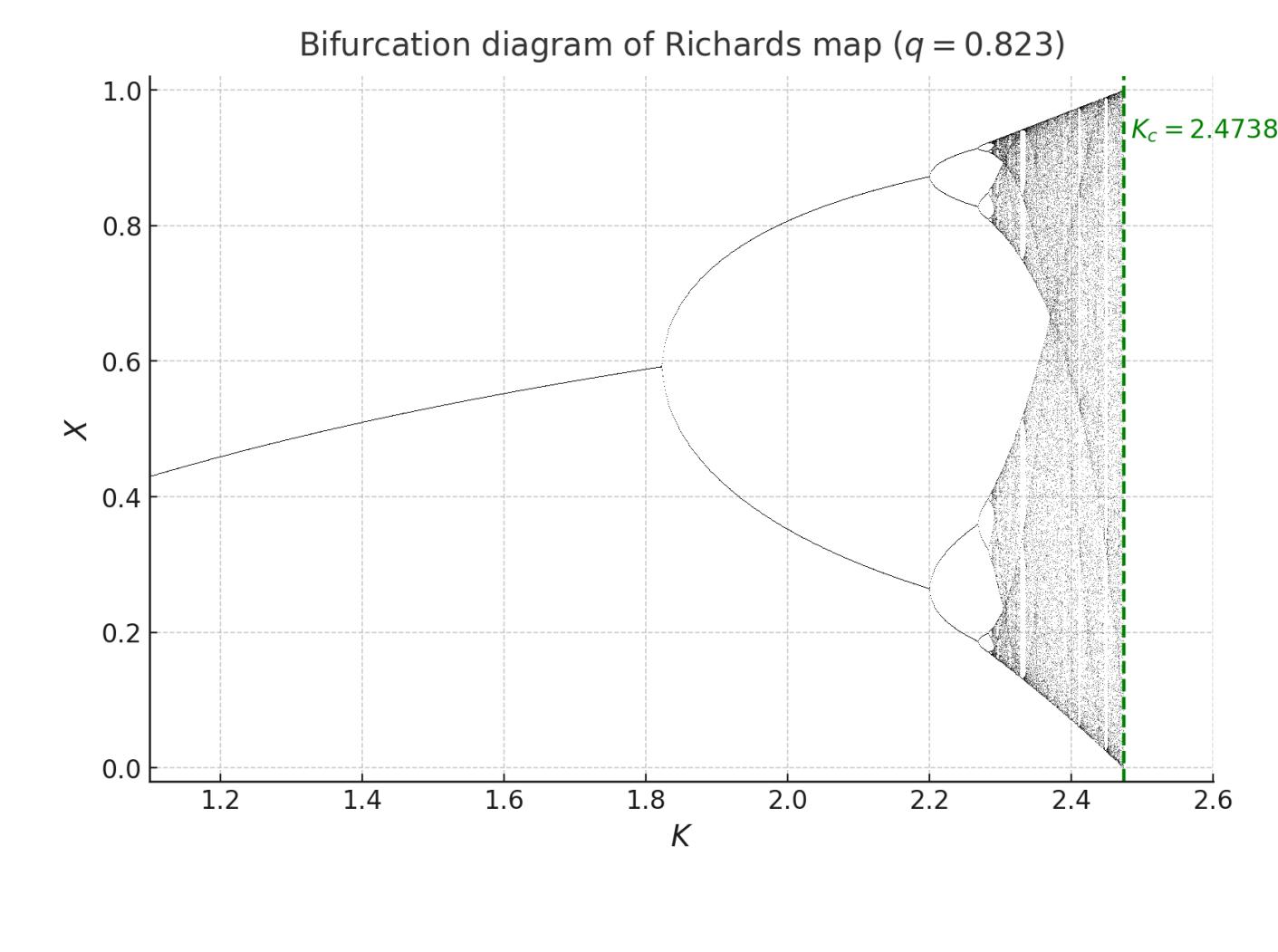
The "sigmoidness" of a sigmoid curve can be measured from the deviations from the line $y = x$! Only the inflection points of the Richards model are lying strictly on it!



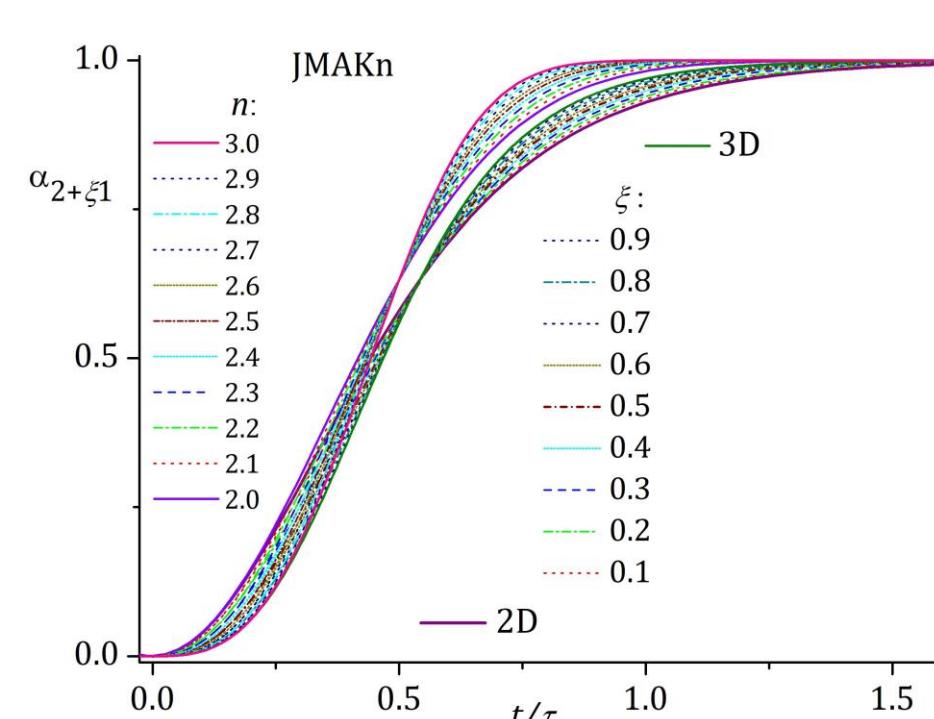
The so called Avrami coordinates reveal the differences between JMAK and the Richards model in fitting α_{21}



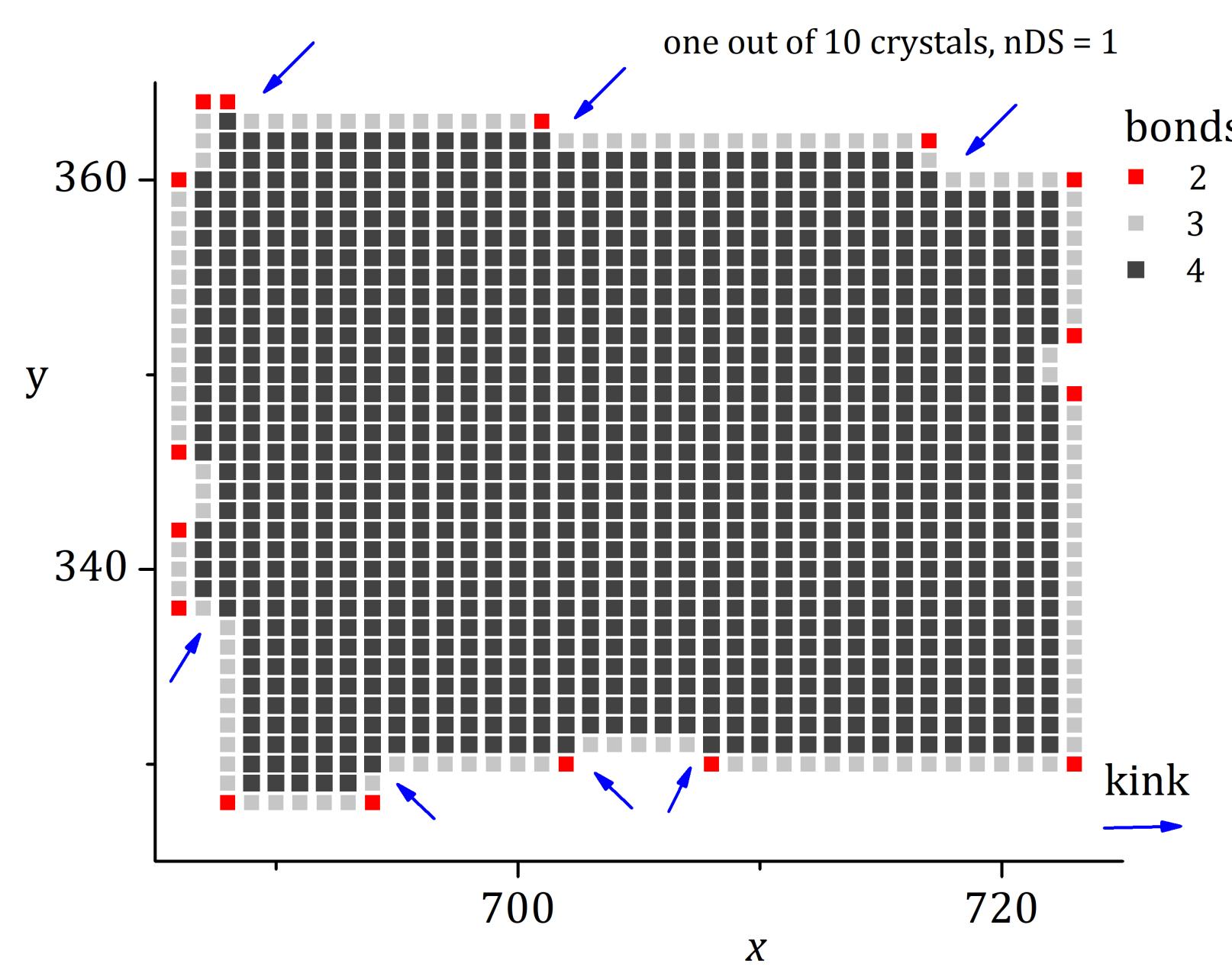
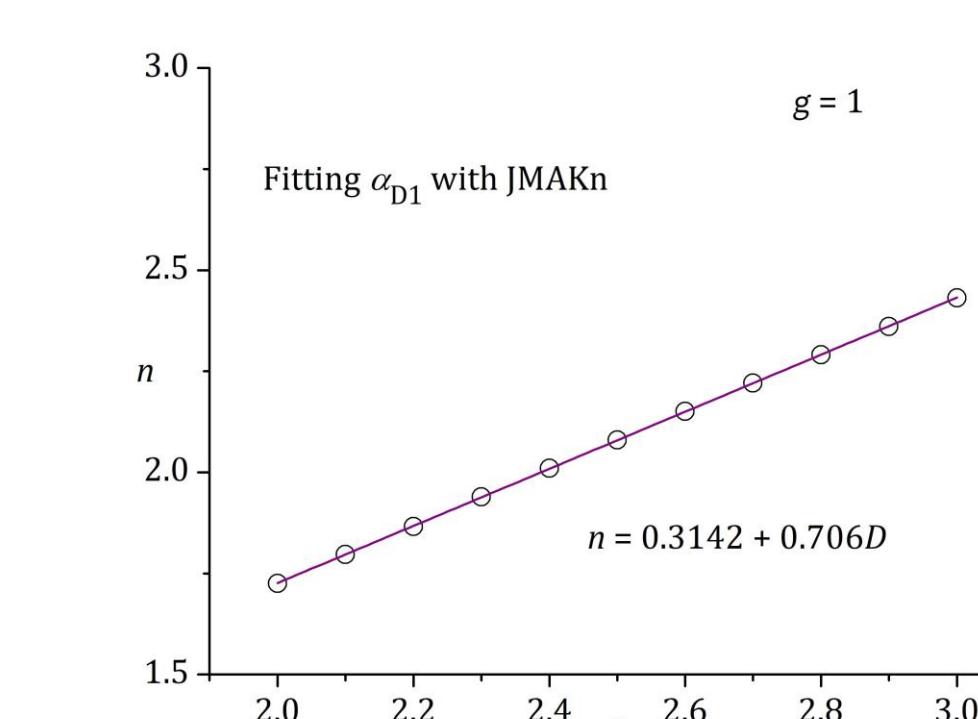
The Richards model is providing a family of curves with same q (here d) that show a catastrophe at certain value of K



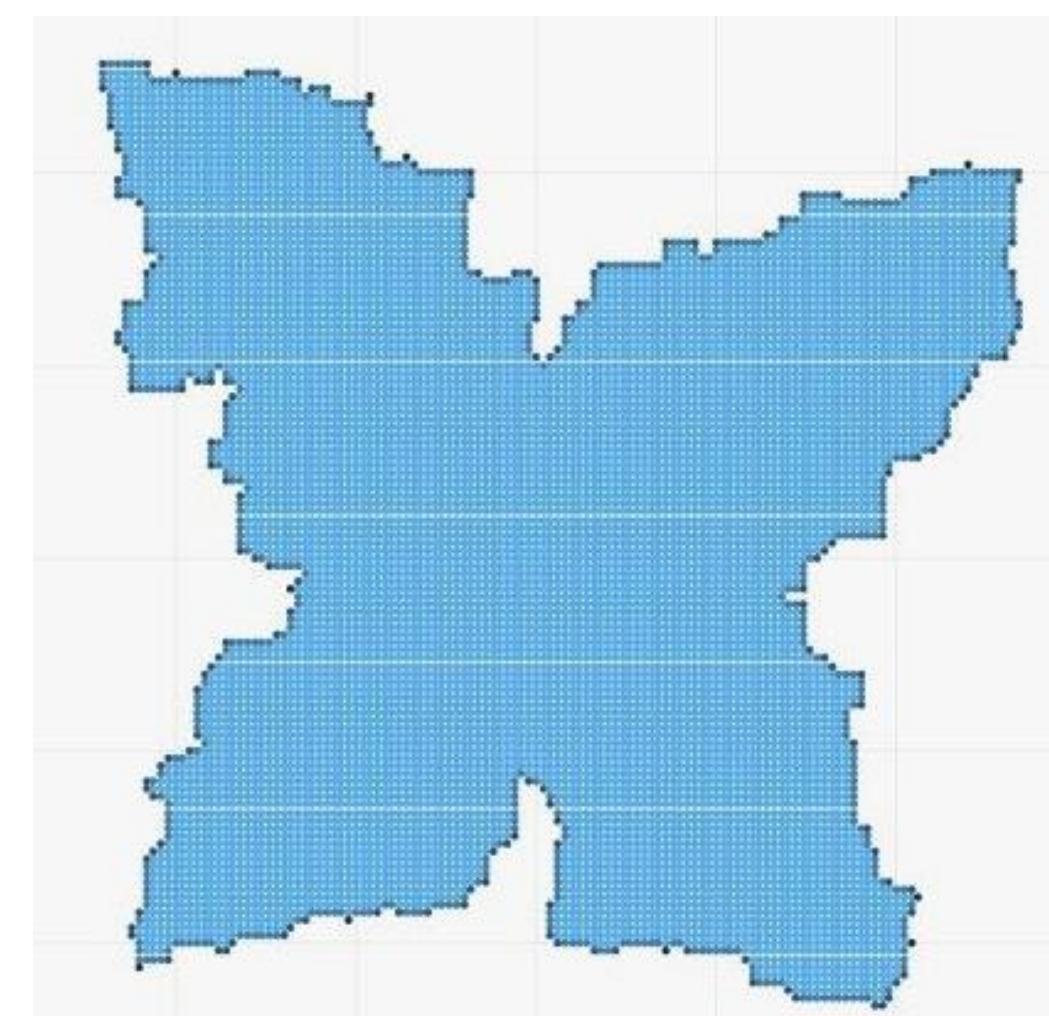
Same value of K is the point of the fully developed chaos in the chaotic map with same q (here d)



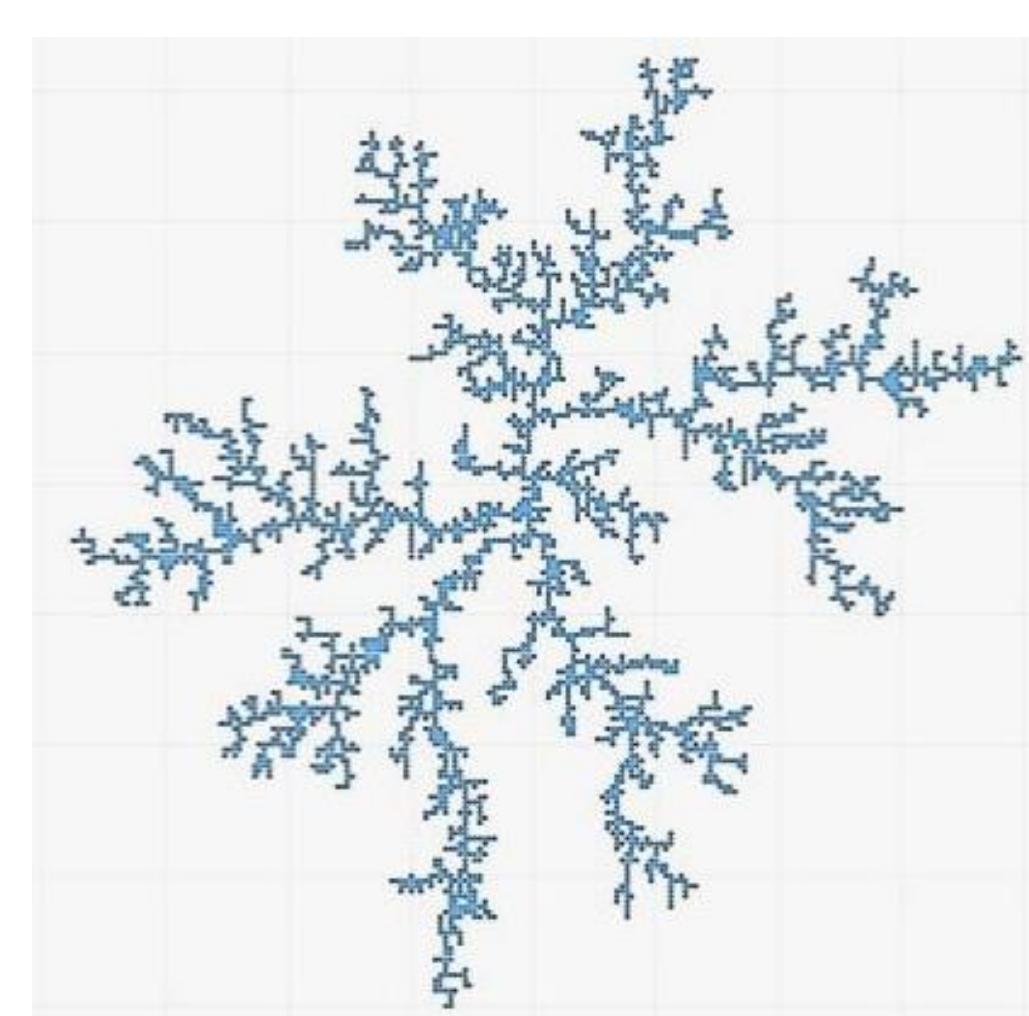
Growth between 2 and 3D



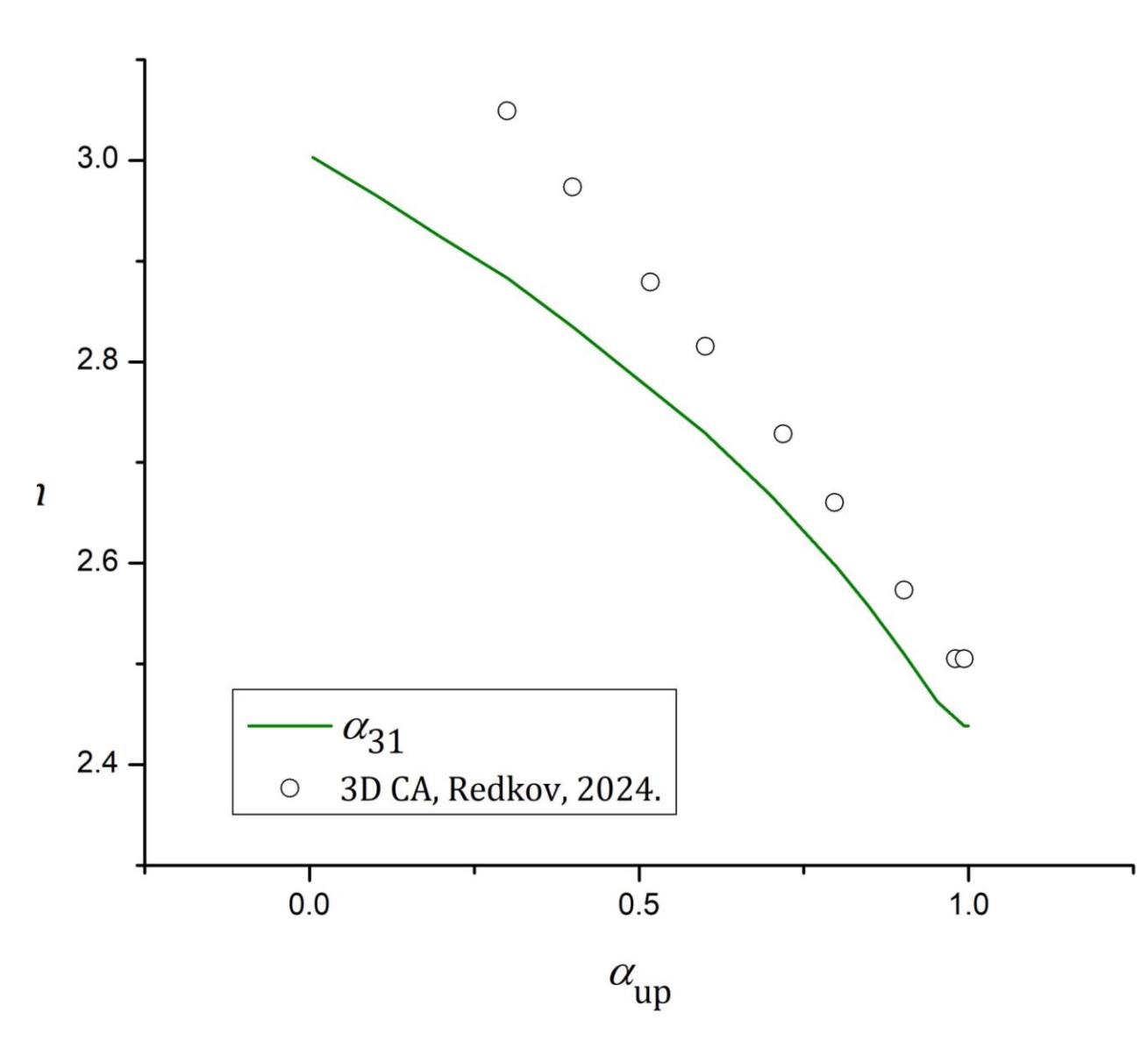
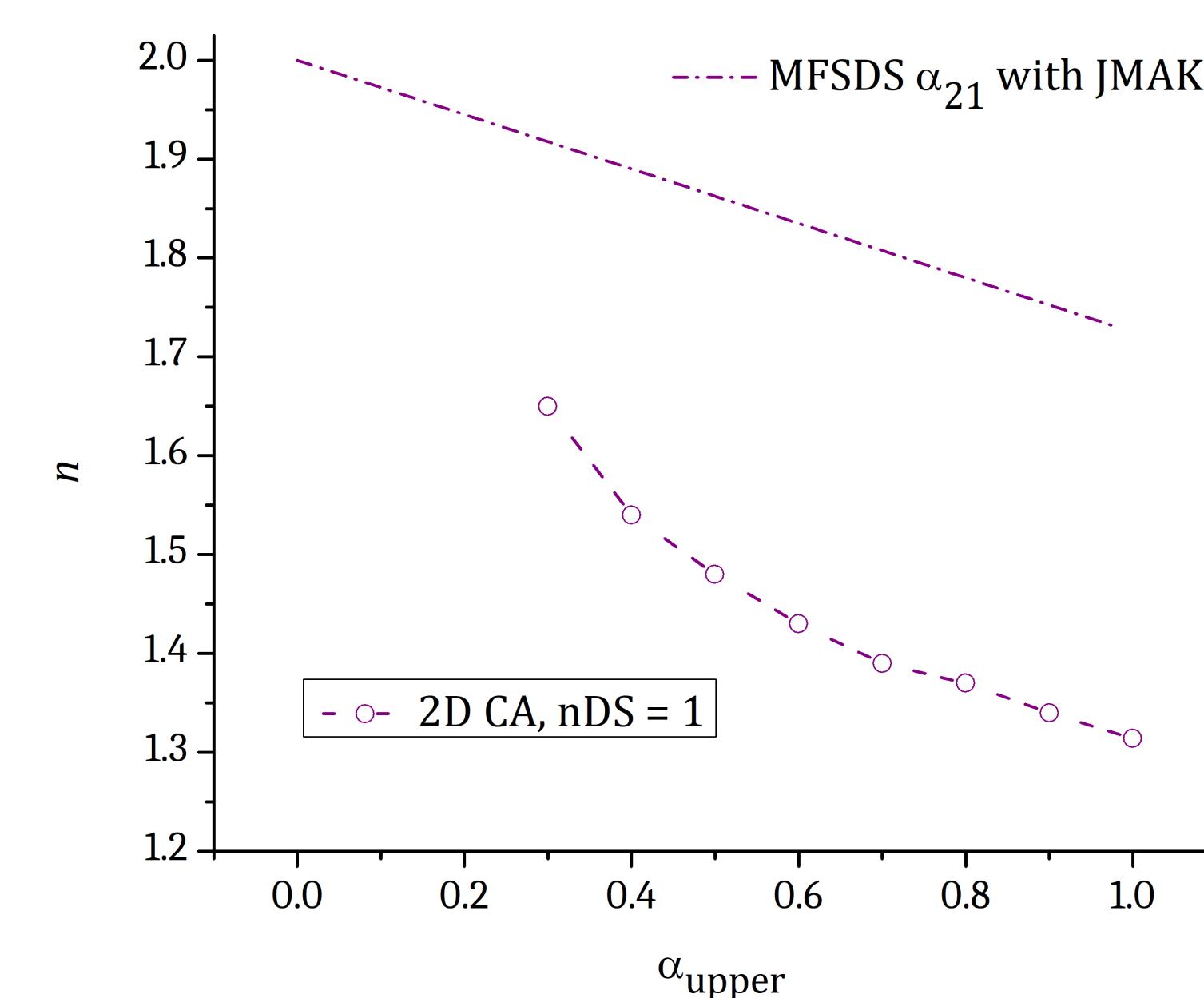
Cellular Automata in 2D are based on attachment rules: to kink position in 2D A2K and to single particle (A21)



A2K results in a dendrite



A21 results in a fractal cluster



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