Protein-film voltammetry: A theoretical study of the temperature effect using square-wave voltammetry

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1. Introduction

Modern voltammetric techniques have tremendous practical applications in biological, pharmaceutical and environmental chemistry [1,2]. The voltammetric techniques have successfully been used to develop various methodologies for quantifying and studying the mechanistic pathways of numerous important bioactive compounds in artificial and biological matrices [3,4]. Application of voltammetry for probing the chemistry of redox proteins has recently emerged as an especially simple and powerful method of investigating biologically relevant redox-active compounds [5–8]. By simple adsorption of the redox protein sample onto the surface of some suitable lipophilic electrode, insights into the processes of electron transfer and protein–protein interactions can be obtained from experiments performed in common voltammetric setup [5–8]. Very often, the protein-film voltammetry is performed with fast-scan rates, which allows to get access to the coupled reactions taking place in the system even in the sub-millisecond timescale. Within the last 10 years, low temperature voltammetry became a popular technique for various purposes. Studying the electrochemical processes at lowered temperatures is important for a better understanding of the mechanistic pathways of many systems [6,9]. Low temperature voltammetry has also been a very useful technique for studying thermally unstable species, detecting electrochemically produced intermediates, and probing the redox reactions in solvents with very low polarity [9–13]. The possibility of studying the electrochemical features of different electrolytes at lowered temperatures attracts also huge attention in the fields of lithium-ion batteries [2,14]. The low temperature voltammetry is currently seen as a powerful alternative to fast-scan protein-film voltammetry [6,15–17]. By performing experiments in partially organic solvent mixtures at temperatures lower than −90 °C, one can slow down the chemical reactions associated with electron transfer at the protein redox active sites and study these reactions using slower scan-rates [9]. The behaviour of the systems studied in this way mimics that observed in fast-scan experiments at room temperature.

We present theoretical results about the behaviour of the square-wave voltammograms of a simple surface redox reaction as a function of the temperature. Square-wave voltammetry was chosen, since it is the most advanced and most sophisticated technique of the pulse voltammetric techniques [2]. The surface redox reactions are regarded as an adequate model for protein-film voltammetric experiments, in which the redox active proteins and the products of their electrochemical transformation are strongly adsorbed on the surface of the working electrode. To the best of our knowledge, there is no theoretical study considering the effect of temperature under voltammetric conditions. Our simulations should help to better...
understand the redox mechanisms, kinetics and thermodynamic parameters of electron transfer reactions in protein-film chronocoulometry and other surface-confined redox systems.

2. Mathematical model and simulation details

The considered surface redox system in this work is described by the following reaction scheme:

\[ A_{(ads)} + n e^- \rightarrow B_{(ads)} \]  

in which the charge of the species is omitted. It is assumed that all participants of the reaction are irreversibly immobilized (adsorbed) on the electrode surface. During the voltammetric experiment the mass transport of all species is neglected. The electrode mechanism is mathematically represented by the following set of equations

\begin{align}
\frac{d\Gamma(A)}{dt} &= -I/(nFS) \\
\frac{d\Gamma(B)}{dt} &= I/(nFS) \\
I &= \{0; \Gamma(A) = \Gamma^*; \Gamma(B) = 0\} \\
t > 0; \Gamma(A) + \Gamma(B) = \Gamma^* 
\end{align}

\( \Gamma \) is a symbol of the surface concentration of particular specie that is a function of time \( t \). \( \Gamma^* \) is the total surface concentration of all species. \( I \) is the symbol of the current, \( S \) is the electrode surface area, \( F \) is the Faraday constant, while \( n \) is a number of exchanged electrons in an elementary act of electrochemical transformation. The solutions for the concentration of the electroactive species A and B are:

\[ \Gamma(A) = \Gamma^* \int_0^t \frac{I}{nFS} \, d\tau \]

\[ \Gamma(B) = \int_0^t \frac{I}{nFS} \, d\tau \]

Considering the Butler–Volmer formalism, at the electrode surface the following condition applies:

\[ \frac{I}{nFS} = k_e \exp(-\alpha\phi) |\Gamma(A) - \exp(\phi)|\Gamma(B)| \]

where \( k_e \) (s\(^{-1}\)) is the heterogeneous electron exchange rate constant corresponding to the standard redox potential \( E_{A/B} \) of the electrode reaction, \( \alpha \) is the cathodic electron transfer coefficient, and \( \phi = \frac{E - E_{A/B}}{nF} \) is the dimensionless relative electrode potential. According to the simple transition state theory, the standard rate constant can be defined as:

\[ k_0 = A \exp(-E_a(RT)^{-1}) \]

where \( A \) is the frequency factor and \( E_a \) is the activation free energy of activated complex [3]. Substituting Eqs. (5) and (6) into the Eq. (7) yields:

\[ \frac{I}{nFS} = k_e \exp(-\alpha\phi) \left[ \Gamma(A)^{\alpha} - \int_0^t \frac{I}{nFS} \, d\tau - \exp(\phi) \int_0^t \frac{I}{nFS} \, d\tau \right] \]

Integral Eq. (8) is a general mathematical solution of the simple surface electrode mechanism. Numerical solution of the Eq. (8) adopted for SWV was obtained according to the method of Nicholson and Olmstead [18]. For numerical solution the time increment \( d \) was defined as \( d = 1/(50\tau) \), where \( f \) is the frequency of the potential modulation. It means that each SW half-period \( \tau/2 \) was divided into 25 increments. The numerical solution reads:

\[ \Psi_m = \frac{Ke^{-\alpha\phi}}{1 + \exp(-2\alpha\phi)} \]

Here, \( K \) is the dimensionless electrode kinetic parameter, defined as \( K = A \exp(-E_a(RT)^{-1}) \), while \( \Psi \) is the dimensionless current defined as \( \Psi = \frac{I}{nFS} \).

Theoretical net SW voltammograms are bell-shaped curves characterized by peak potential \( \Delta E_p \), peak current \( \Psi_p \), and half-peak width \( \Delta E_{p/2} \). By \( \Psi_{red} \) and \( \Psi_{ox} \) we assign the cathodic (reduction) and anodic (oxidation) currents of the voltammograms, respectively. All these parameters of the voltammetric curves are mainly dependent on the potential modulation parameters (frequency \( f \), amplitude \(-E_{red}\) and potential increment \( \Delta E \)), as well as on the dimensionless redox kinetic parameter \( K \), the number of exchanged electrons \( n \), the electron transfer coefficient \( \alpha \), and the temperature \( T \). Detailed studies of the features of simple surface redox reaction as a function of the kinetic parameter \( K \), \( E_{red} \), \( \alpha \), and \( n \) under conditions of square-wave voltammetry can be found elsewhere [2,19,20]. In this communication we only focus on the influence of the temperature to the main attributes of the square-wave voltammograms of a simple surface redox reaction. All the simulations have been performed with help of the MATHCAD software.

From Eq. (9) follows that temperature affects the voltammetric response through two parameters, i.e., the relative dimensionless potential \( \phi \) and the electrode kinetic parameter \( K \). By varying the temperature, the two mentioned parameters are simultaneously altered. To understand the influence of each parameter separately, in the first set of simulation results presented in the following subsections 3.1 to 3.3 (Figs. 1–7), it is assumed that the electrode kinetic parameter \( K \) is constant, and the temperature affects only the parameter \( \phi \). This type of simulations corresponds to a comparison of the following conditions:

\begin{align}
\text{condition 1:} & \quad \phi_1 \quad T = 298K \\
\text{condition 2:} & \quad \phi_2 \quad T = 298K \\
\text{condition 3:} & \quad \phi_1 \quad T = 298K \\
\text{condition 4:} & \quad \phi_2 \quad T = 298K \\
\end{align}

Fig. 1. Slow electron transfer: square-wave voltammograms simulated for different temperatures. The simulation parameters are: dimensionless kinetic parameter \( K = 0.001 \), square-wave amplitude \( E_{sw} = 50 \text{ mV} \), potential increment \( \Delta E = 2 \text{ mV} \), number of exchanged electrons \( n = 1 \), and electron transfer coefficient \( \alpha = 0.5 \).
different experimental systems, which have identical electrode kinetic parameters at a particular temperature. The results presented in the subsection 3.4 correspond to the analysis of a single surface electrode reaction, during which the temperature influences the two parameters $\phi$ and $K$ simultaneously.

3. Results and discussion

3.1. Irreversible electron transfer

In the region of very sluggish (irreversible) electron transfer, i.e., the value of the dimensionless kinetic parameter $K$ falls within the interval $-2 < \log(K) < -0.5$, all the features of the theoretical square-wave voltammograms of a simple surface redox reaction are strongly affected by the temperature (see Fig. 1). Evidently, for a given square-wave amplitude $E_{sw}$ and electron transfer coefficient $\alpha$, decreasing the temperature increases the electrochemical reversibility of the simulated voltammograms. This effect is represented in augmentation of the magnitudes of both oxidation and reduction current components. In the same time, lowering of the temperature produces an effect to the shape of the backward current component that starts getting a form and sign typical for quasireversible redox systems.

The net peak currents of the theoretical voltammograms increase exponentially by decreasing of $T$ (see Fig. 2A). As the temperature is incorporated in the exponential term of the current-potential interdependence of the Butler–Volmer equation applied to the considered system (see Eq. (7)), this feature was expected. Besides, the net peak potentials of theoretical SW voltammograms ($\Delta E_p$) shift linearly in negative direction by increasing of the temperature (see Fig. 2B). The linear dependence between $\Delta E_p$ and $T$ is represented as $\Delta E_p = (-\frac{zF}{nF})T$, where the constant $c$ in the slope is a function of the square-wave amplitude, while $R$, $n$ and $F$ are the universal gas constant, number of the exchanged electrons, and the Faraday constant, respectively.

Another very relevant parameter of square-wave voltammograms is the half-peak width $\Delta E_{p/2}$. The half-peak width is also dependent on temperature in case of very slow electron transfer as shown in Fig. 3. $\Delta E_{p/2}$ decreases linearly with decreasing temperature, with a slope being inversely proportional of $\alpha$. The dependence $\Delta E_{p/2}$ vs $T$ in the irreversible region is given as $\Delta E_{p/2} = (\frac{zF}{nF})T$, where the factor $z$ is a constant depending on $E_{sw}$. A very important result in this set of simulations is the independence of the half-peak width $\Delta E_{p/2}$ on the kinetic parameter $K$ ($K = k_0/k_f$), in the regions of $K < 0.005$ [2]. This feature allows a very easy calculation of $\alpha$. If we bring the redox reaction in the irreversible region (by increasing of the SW frequency), and if $\Delta E_{p/2}$ is analyzed as function of $T$, it is possible to estimate the value of electron transfer coefficient $\alpha$ through comparison of the experimental slope with the theoretical ones shown in Fig. 3.

3.2. Quasireversible electron transfer

In case the value of the dimensionless kinetic parameter $K$ falls within interval $-2 < \log(K) < 0.5$, the reaction is in the region of “quasireversible electron transfer” [2,19,21]. The effect of the temperature on theoretical square-wave voltammograms in the quasireversible region is presented in Fig. 4. Simulations show that one distinctive attribute in this region is the very slight temperature dependence of the SW net peak potentials. This is basically the opposite behaviour to that observed in the region of irreversible electron transfer. The temperature, however, has a big influence to the shape of the oxidation and reduction components of the SW voltammograms; the widths of them are getting narrower if lowering the temperature. At very low temperatures, the net peak of the SW voltammogram even splits up in two peaks. The splitting of the net peak is usually caused by the skew of forward and backward current components on the potential scale, as the value of the dimensionless kinetic parameter $K$ increases [2,19]. The splitting effect is a feature of the surface redox reactions exhibiting very fast electron transfer. This phenomenon is discussed in details elsewhere [2]. Nevertheless, it is clear from the voltammograms in Fig. 4 that lowering the temperature in the system leads to an increase of its electrochemical reversibility.

In Fig. 5A and B, we simulated the temperature influence on the peak currents and the half-peak widths of the net theoretical voltammograms. Similarly to the region of irreversible electron transfer, the net SW peak currents rise exponentially with decreasing temperature (Fig. 5A). The magnitudes of the half-peak widths are again a linear function of the temperature, but the slopes are basically independent of $\alpha$ (Fig. 5B). The independence of the slope $\Delta E_{p/2} = \alpha T$ on $\alpha$ distinguishes the quasireversible electron transfer from irreversible electron transfer (compare Figs. 5B and 3). At this stage, it is worth mentioning that for a given temperature, the half-peak widths of theoretical square-wave voltammograms are linear functions of the logarithm of the dimensionless kinetic parameter $K$ (in the region $-2 < \log(K) < 0.5$). This property is considered to be very useful for the determination of the standard rate constant of electron transfer, and it is discussed in detail in our concurrent paper (submitted).
The most remarkable attribute of the simple surface redox reaction studied under conditions of square-wave voltammetry is the parabolic dependence of the dimensionless peak current on the magnitude of the kinetic parameter $\log(K)$ \[2,20\]. This feature is known as “quasireversible maximum”, and it has been widely explored for estimation of the kinetics constant of electron transfer of various redox systems \[5,20,22\]. The redox reactions featuring moderate electron transfer (i.e. the quasireversible ones) usually give responses that are many times larger than much faster (reversible) reactions. This is mainly a consequence of the current sampling procedure that is used in pulse voltammetric techniques, but can also be attributed to the specific chronoamperometric properties of the surface redox reaction \[2\]. In Fig. 6, we simulated the dependence of the SWV net peak currents on $\log(K)$ for different temperatures. Generally, the position of the maximum is a function of the temperature, shifting towards lower values of $K$ with decreasing $T$. Up to temperatures of approximately 350 K, there is a linear dependence between the $\log(K)$ and the temperature corresponding to the maximums of the curves in Fig. 6 (see inset in Fig. 6). The results presented in Fig. 6 demonstrate that variation of the temperature in the electrochemical cell can considerably change the reversibility of the redox system.

3.3. Very fast electron transfer

One of the most interesting items of the surface redox reaction of a strongly adsorbed redox couple is the “splitting of the net SW response” \[19,23\]. Commonly, for the values of the dimensionless parameter $\log(K)>0.6$ (i.e. very fast electron transfer) the net SW peak splits into two peaks that are symmetrically positioned around the standard redox potential. The large separation of the forward and backward current components is a consequence of the big values of the dimensionless rate constants of the oxidation and reduction half-reactions and the specific way of current sampling in square-wave voltammetry \[2,19,23\]. Experimentally, the splitting phenomenon can be achieved by decreasing the square-wave frequency or by increasing the SW amplitude \[2,23\]. The potential separation between the separated peaks is a function of the dimensionless kinetic parameter $K$, but also of the square-wave amplitude $E_{sw}$. The features of the splitting phenomenon are discussed in detail elsewhere \[23\], and a very simple and powerful methodology for complete thermodynamic and kinetic characterization of surface redox reactions is available \[2,23\]. The effect of the temperature on the SW voltammograms featuring fast electron transfer is shown in Fig. 7. By decreasing the temperature from 298 to 100 K, a slight increase in the potential separation between the split SW peaks can be observed. The width of the twin peaks is, however, very sensitive to the temperature changes,
getting much narrower by decreasing the temperature. At very low
temperatures, the twin peaks are finally seen as narrow spikes. This is
a very specific voltammetric situation, and it can sometimes lead to
wrong conclusions, especially if the properties of the surface redox
reactions under conditions of square-wave voltammetry are not well
known. The features of the SW voltammograms presented in Fig. 7
should avoid the dangers of invoking multiple species, “stable
radicals”, or additional processes to explain “odd” features met in
some studies, such as appearance of multiple peaks or very narrow
peaks [24–33], particularly in SW voltammetric studies performed
under cryogenic conditions.

3.4. Analysis of the temperature effect relevant to the study of a single
electrode reaction

The voltammetric response of a single electrode reaction is an item of
great interest. Therefore, we have analyzed its temperature dependence.
As mentioned earlier, Eq. (9) explicitly shows that the temperature
affects the voltammetric responses through two parameters, i.e., the
relative dimensionless potential \( \phi \) and the dimensionless electrode
kinetic parameter \( K \), which are altered simultaneously by varying \( T \). The
temperature effect on the value of the standard rate constant of electron
transfer is commonly represented in the Arrhenius form, i.e.:

\[
\ln k = \ln k_0 - \frac{E_a}{R \cdot T}
\]

(8)

where \( k \) is the electron transfer rate constant, \( k_0 \) is the rate
constant at reference temperature, \( E_a \) is the activation energy,
\( R \) the gas constant, and \( T \) the temperature in Kelvin.

It is important to note, that for a given temperature, the
“quasireversible maximum” appears when the SW frequency of the
signal fulfills the condition: \( f_{\text{max}} = f_{\text{max}}^{1/2} \exp \left[-\frac{E_a}{R \cdot T} \right] \). From this
expression, it follows that the maximal SW frequency \( f_{\text{max}} \), at which
the “quasireversible maximum” appears, is given by:

\[
\ln[f_{\text{max}}] = \ln(A) - \ln(K_{\text{max}}) - \left(\frac{E_a}{R \cdot T}\right)^{-1}
\]

(11)

The last equation is of great importance, since it permits to
determine the frequency factor of the electron transfer reaction \( A \)

\[
f_{\text{max}}(\Delta) = 55
\]

Fig. 7. Fast electron transfer: square-wave voltammograms simulated for different temperatures. The simulation parameters are: dimensionless kinetic parameter \( K = 11 \), square-wave amplitude \( E_{\text{sw}} = 50 \text{ mV} \); potential increment \( \Delta E = 2 \text{ mV} \), and electron transfer coefficient \( \alpha = 0.5 \).

Fig. 8. A) Temperature effect to the theoretical “quasireversible maximums” simulated under “Arrhenius” conditions. B) shows the dependence between the logarithm of the values of the frequencies corresponding to the maximums of the parabolic curves—\( \log(f_{\text{max}}) \) and the inverse values of the temperatures \( 1/T \) (see Fig. 8B). The linear dependence between \( \log(f_{\text{max}}) \) and \( 1/T \) has the following form:

\[
\log(f_{\text{max}}) = -934.02 T^{-1} + 5.6733
\]

(10)
In one practical example, we show how the thermodynamic parameters of the electron transfer reaction can be estimated with this methodology. By exploring the value of the log(Kmax)=0 at T=300 K (see inset from Fig. 6), with the help of the equation of the linear dependence log(Kmax)=−T (Eqs. (10) and (11)), we estimated the values of $E_f$ and $A$ being 17,900 J mol$^{-1}$ and 5.7×10$^5$ s$^{-1}$, respectively. The value of $E_f$ and $A$ have been identified from the Eq. (11). These estimated values for $E_f$ and $A$ are in very good agreement with the values used for the simulations of Fig. 8 ($E_f$=20,000 J mol$^{-1}$, and $A=10^5$ s$^{-1}$), a fact that shows the reliability of the proposed methodology. It should be also mentioned that the electron transfer activation energy $E_f$ is closely connected to the standard redox potential of the investigated redox compounds [3]. The last Fig. 8A and B show that the temperature effect on the phenomenon of “quasireversible maximum” can be viewed as a simple and viable way to precisely estimate the thermodynamic parameters as the standard redox potentials of lipophilic proteins and other surface-active redox compounds.

4. Conclusions

In this paper we analyzed the effect of the temperature on theoretical square-wave voltamograms of a surface redox reaction, which is considered as an adequate model of protein-film voltammetric experiments. Protein-film voltammetry is a relatively new concept, which offers many interesting opportunities for fundamental and applied research. Being extensively explored to investigate the kinetics of electron transfer and protein–protein interactions in various scenarios, the protein-film voltammetry appears to be a very simple and efficient tool to understand the redox properties of various enzymes.

Electron transfer reactions are central to the function of proteins in many biological processes. This is well known in bioenergetics: photosynthesis and respiration realize energy conversion through a complex sequence of electron transfer reactions. However, electron transfer also takes place in many other biological processes ranging from cell defense to gene control. The rate of electron transfer from a donor D to an acceptor A is a key parameter that determines biological function, and much effort has been made to relate the rate of electron transfer to structural and thermodynamic features of the compounds of interest. In the last two decades, square-wave voltammetry has emerged as one of the leading voltammetric techniques in respect of the kinetics characterization of chemical and electron transfer steps by various surface electrode reactions [2,35]. It offers relative simple modes for recognition of the electrode mechanisms, as well as for measuring their kinetics [2,35–41].

We have analyzed temperature effects to the protein-film square-wave voltammetric responses featuring slow, quasireversible and fast electron transfer. Generally, by decreasing the temperature of the system, an increase of the electrochemical reversibility of the surface redox systems has been observed. In the region of very slow electron transfer, the magnitude of the half-peak width of the theoretical SW voltammograms decreases linearly with decreasing the temperature. The slope of half-peak width against $T$ was found to be inversely proportional to the electron transfer coefficient $\alpha$. The slope of $\Delta E_{p/2}$ vs. $T$ was, however, independent on the kinetic parameter $K$ if the value of $K$ was ≤0.005. This means that the linear dependence between $\Delta E_{p/2}$ and $T$ in the irreversible region (defined as $\Delta E_{p/2} = (2 \frac{R}{\nu F} T)$, where the factor $z$ in the slope is a constant dependent on $E_{con}$) can be used to estimate the electron transfer coefficient $\alpha$.

Lowering the temperature significantly affects the phenomena of the “quasireversible maximum” and “splitting SW peaks”, which are the main kinetic attributes of the surface redox reactions featuring moderate and fast electron transfers [2]. The appearance of the spiky twin peaks by surface redox systems with very fast electron transfer at low temperatures should not be interpreted as an abnormal feature of square-wave voltammetry. Since the surface redox reaction is considered as an adequate model for a protein-film voltammetric experiments, our simulations should help to elucidate the redox mechanisms and to determine the kinetic parameters of protein-film cyclic voltammetry. Moreover, by simulating the temperature effects of the “quasireversible maximum” under “Arrhenius” conditions, i.e. by considering the temperature effects of the standard rate constant of a single electrode reaction, we have shown how elegantly one can calculate important thermodynamic parameters of the surface-confined electron transfer reactions. We give in this work a theoretical equation (Eq. (12)) from which one can calculate the critical value of the kinetic parameter corresponding to the quasireversible maximum $K_{max}$ at a given temperature. In the real experiment, the quasireversible maxima presented in Fig. 8A could be demonstrated by varying the SW signal frequency. Plotting the ratio of the real peak current and the corresponding frequency $\nu_{sw}$ versus the logarithm of the signal frequency $\log(\nu)$ at several temperatures, one could reconstruct the theoretical dependences depicted in Fig. 8A. If the critical frequencies associated with the quasireversible maxima $f_{max}$ are obtained experimentally from the parabolic curves $I_{p/2}$ vs. log $f$, and if the critical values of the kinetic parameter $K_{max}$ at a given temperature are calculated theoretically by using Eq. (12), then, by plotting the dependence between the critical values of the estimated frequencies $\log(f_{max})$ vs. $\nu_{sw}$ one should get a linear regression line as presented in Fig. 8B. The slope of this linear dependence allows to obtain the value of the activation energy of electron transfer $E_a$, while the frequency factor of the electron transfer reaction $A$ can be determined from the interception (see Eq. (11)). To the best of our knowledge, this is the first theoretical work under conditions of SWV, which shows that the “quasireversible maximum” can be explored to determine the activation energy of electron transfer reactions in surface redox systems, and consequently, for the determination of the standard redox potential of many surface-active compounds. These calculations unanimously show that the phenomenon of “quasireversible maximum” can be explored simultaneously for both, the kinetic and the thermodynamic characterization of the electron transfer steps during surface redox reactions.

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